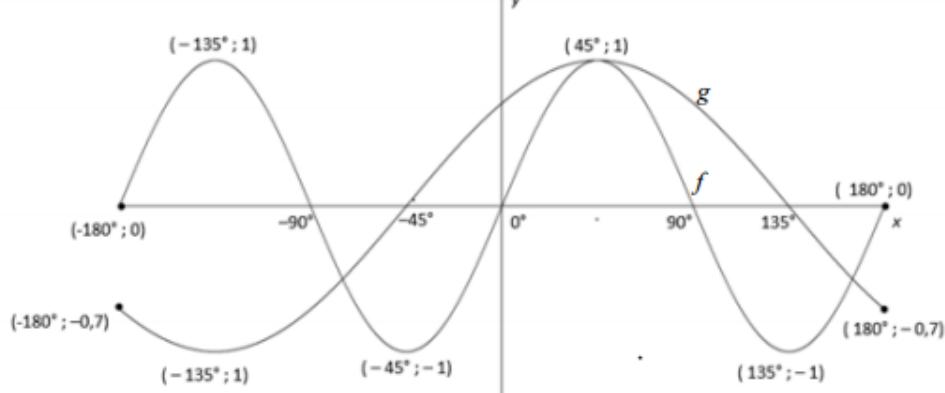


QUESTION/VRAAG 5

5.1



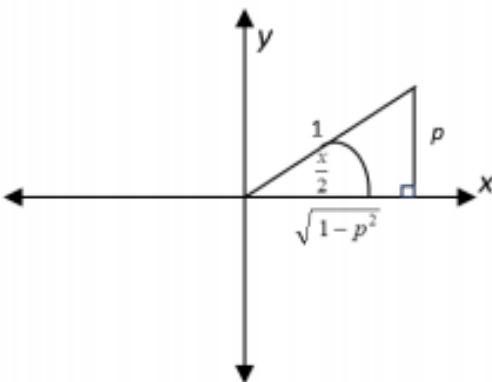
- ✓ turning points/draaipunte
 - ✓ x -intercepts/ x -afsnitte
 - ✓ end points/eindpunte
- (3)

5.2.1	$\sin 2x = \cos(x - 45^\circ)$ $\sin 2x = \sin[90^\circ - (x - 45^\circ)]$ $\sin 2x = \sin(135^\circ - x)$ $2x = 135^\circ - x + k \cdot 360^\circ; k \in \mathbb{Z}$ $3x = 135^\circ + k \cdot 360^\circ; k \in \mathbb{Z}$ $x = 45^\circ + k \cdot 120^\circ; k \in \mathbb{Z}$	$\checkmark \sin 2x = \sin[90^\circ - (x - 45^\circ)]$ $\checkmark 2x = 135^\circ - x + k \cdot 360^\circ; k \in \mathbb{Z}$ $\checkmark x = 45^\circ + k \cdot 120^\circ; k \in \mathbb{Z}$
	OR/OF $2x = 180^\circ - (135^\circ - x) + k \cdot 360^\circ; k \in \mathbb{Z}$ $2x = 45^\circ + x + k \cdot 360^\circ; k \in \mathbb{Z}$ $x = 45^\circ + k \cdot 360^\circ; k \in \mathbb{Z}$ $x \in \{45^\circ; 165^\circ\}$	$\checkmark 2x = 180^\circ - (135^\circ - x) + k \cdot 360^\circ; k \in \mathbb{Z}$ $x = 45^\circ + k \cdot 360^\circ; k \in \mathbb{Z}$ $\checkmark k \in \mathbb{Z}$ $\checkmark x = 45^\circ$ $\checkmark x = 165^\circ$
	OR/OF $\sin 2x = \cos(x - 45^\circ)$ $\cos(90^\circ - 2x) = \cos(x - 45^\circ)$ $90^\circ - 2x = x - 45^\circ + k \cdot 360^\circ; k \in \mathbb{Z}$ $-3x = -135^\circ + k \cdot 360^\circ; k \in \mathbb{Z}$ $x = 45^\circ + k \cdot 120^\circ; k \in \mathbb{Z}$	$\checkmark \cos(90^\circ - 2x) = \cos(x - 45^\circ)$ $\checkmark -3x = -135^\circ + k \cdot 360^\circ; k \in \mathbb{Z}$ $\checkmark x = 45^\circ + k \cdot 120^\circ; k \in \mathbb{Z}$
	OR/OF $90^\circ - 2x = 360^\circ - (x - 45^\circ) + k \cdot 360^\circ; k \in \mathbb{Z}$ $90^\circ - 2x = 360^\circ - x + 45^\circ + k \cdot 360^\circ; k \in \mathbb{Z}$ $-x = 315^\circ + k \cdot 360^\circ; k \in \mathbb{Z}$ $x = -315^\circ + k \cdot 360^\circ; k \in \mathbb{Z}$ $x \in \{45^\circ; 165^\circ\}$	$\checkmark 90^\circ - 2x = 360^\circ - (x - 45^\circ) + k \cdot 360^\circ; k \in \mathbb{Z}$ $x = -315^\circ + k \cdot 360^\circ; k \in \mathbb{Z}$ $\checkmark k \in \mathbb{Z}$ $\checkmark x = 45^\circ$ $\checkmark x = 165^\circ$
5.2.2	$x \in \{15^\circ; 135^\circ\}$	$\checkmark x = 15^\circ$ $\checkmark x = 135^\circ$
5.2.3	$x \in (165^\circ; 180^\circ)$	(2)
	OR/OF $165^\circ < x < 180^\circ$	$\checkmark \checkmark$ critical values & notation/kritiese waardes en notasie
5.3	360°	\checkmark answer/antwoord
5.4	$\sqrt{2} \sin 2x = \cos x + \sin x$ $\sin 2x = \frac{\cos x + \sin x}{\sqrt{2}}$ $\sin 2x = \frac{1}{\sqrt{2}} \cos x + \frac{1}{\sqrt{2}} \sin x$ $\sin 2x = \cos x \cos 45^\circ + \sin x \sin 45^\circ$ $\sin 2x = \cos(x - 45^\circ)$ $f(x) = g(x)$	$\checkmark \sin 2x = \frac{\cos x + \sin x}{\sqrt{2}}$ $\checkmark \sin 2x = \frac{1}{\sqrt{2}} \cos x + \frac{1}{\sqrt{2}} \sin x$ $\checkmark \sin 2x = \cos x \cos 45^\circ + \sin x \sin 45^\circ$
		(3)
		[18]

QUESTION/VRAAG 6

<p>6.1.1</p> $\tan \theta = \frac{-2}{-1} = 2$	<ul style="list-style-type: none"> ✓ $x = -1$ ✓ answer/antwoord (2)
<p>6.1.2</p> $\begin{aligned} \cos 2\theta &= 2\cos^2 \theta - 1 \\ &= 2\left(\frac{-1}{\sqrt{5}}\right)^2 - 1 \\ &= \frac{-3}{5} \end{aligned}$ <p>OR/OR</p> $\begin{aligned} 1 - 2\sin^2 \theta &= 1 - 2\left(\frac{-2}{\sqrt{5}}\right)^2 \\ &= \frac{-3}{5} \end{aligned}$ <p>OR/OR</p> $\begin{aligned} \cos^2 \theta - \sin^2 \theta &= \left(\frac{-1}{\sqrt{5}}\right)^2 - \left(\frac{-2}{\sqrt{5}}\right)^2 \\ &= \frac{-3}{5} \end{aligned}$	<ul style="list-style-type: none"> ✓ double angle identity/dubbel hoek identiteit ✓ substitution into correct formula/substitusie in korrekte formule ✓ answer/antwoord (3) ✓ double angle identity/dubbel hoek identiteit ✓ substitution into correct formula/substitusie in korrekte formule ✓ answer/antwoord (3) ✓ double angle identity dubbel hoek identiteit ✓ substitution into correct formula/substitusie in korrekte formule ✓ answer/antwoord (3)

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6.2	$ \begin{aligned} & 2 \cos^2 15^\circ - 1 + \frac{2 \sin 140^\circ}{\cos 310^\circ} \\ &= \cos 30^\circ + \frac{(2 \sin 40^\circ)}{(\cos 50^\circ)} \\ &= \frac{\sqrt{3}}{2} + \frac{2 \sin 40^\circ}{\sin 40^\circ} \\ &= \frac{\sqrt{3} + 4}{2} \end{aligned} $	<ul style="list-style-type: none"> ✓ $\cos 30^\circ$ ✓ $\sin 40^\circ$ ✓ $\cos 50^\circ$ ✓ $\sin 40^\circ$ ✓ answer/antwoord (5)
6.3	 $ \begin{aligned} & \sin x - 1 \\ &= 2 \sin \frac{x}{2} \cos \frac{x}{2} - 1 \\ &= 2 \left(\frac{p}{1}\right) \left(\frac{\sqrt{1-p^2}}{1}\right) - 1 \\ &= 2p\sqrt{1-p^2} - 1 \end{aligned} $	<ul style="list-style-type: none"> ✓ $x = \sqrt{1-p^2}$ ✓ double angle/dubbelhoek ✓ substitution/substitusie ✓ answer/antwoord (4)
6.4	$ \begin{aligned} & \frac{3 \sin x + 2(2 \sin x \cos x)}{2 + 3 \cos x + 2(2 \cos^2 x - 1)} \\ &= \frac{\sin x \cdot (3 + 4 \cos x)}{4 \cos^2 x + 3 \cos x} \\ &= \frac{\sin x \cdot (3 + 4 \cos x)}{\cos x \cdot (4 \cos x + 3)} \\ &= \tan x \end{aligned} $	<ul style="list-style-type: none"> ✓ $2 \sin x \cos x$ ✓ $2 \cos^2 x - 1$ ✓ $\sin x (3 + 4 \cos x)$ ✓ $\cos x (4 \cos x + 3)$ ✓ answer/antwoord (4)

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Marking Guidelines/Nasiennriglyne

6.5	$\frac{\sin x + \cos x}{\sin x - \cos x}$ $= \frac{\frac{\sin x}{\cos x} + \frac{\cos x}{\cos x}}{\frac{\sin x}{\cos x} - \frac{\cos x}{\cos x}}$ $= \frac{\tan x + 1}{\tan x - 1}$ $= \frac{\frac{p}{t} + 1}{\frac{p}{t} - 1}$ $= \frac{p+t}{t} \div \frac{p-t}{t}$ $= \frac{p+t}{t} \times \frac{t}{p-t}$ $= \frac{p+t}{p-t}$	✓ divide numerator and denominator by $\cos x$ /deel noemer en teller met $\cos x$ ✓ $\frac{\tan x+1}{\tan x-1}$ ✓ $\frac{p+1}{p-1}$ ✓ $\frac{p+t}{t} \div \frac{p-t}{t}$ ✓ $\frac{p+t}{t} \times \frac{t}{p-t}$ (5)	[23]
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